Frostwing Flat Plate CFD Simulations: Reynolds Number Effect and Boundary Layer Analysis

Pekka Koivisto, Tomi Honkanen, Juha Kivekäs
This research report contains comparison of the flat plate CFD results to the wind tunnel tests with matching fluid and flow properties. The research has been conducted as part of the third year of the Frostwing project.

Three new CFD simulation cases are presented, two with a flat plate length of 0.6 m and one with a length of 1.8 m. The cases simulate Type I de-icing fluid behavior in an accelerating air flow. The fluid properties and the acceleration of the air flow match those present in the wind tunnel experiments used for comparison.

The latest simulation effort has two main objectives. The first is to produce simulation results that could be compared to the results of the wind tunnel experiments. The second objective is to compare the CFD results of the 0.6-meter-long flat plate to the 1.8-meter-long version, especially the first 0.6 meters of it. This is to check if the longer plate has an effect that propagates upstream (Reynolds number effect).

As part of the the Icewing project wind tunnel tests were also done with the flat plate models with a boundary layer pressure-rake instrumentation. A summary of the results of these experiments are presented in this report. The boundary layer data is also compared to the CFD results.
FOREWORD

This research report documents findings of the CFD simulations and wind tunnel experiments of de-icing fluid behavior on a flat plate in an airstream over it. It forms part of the third year of the Frostwing project, performed under a Research agreement between the Federal Aviation Administration FAA and the Finnish Transport safety Agency Trafi together with the National Aviation and Space Administration NASA, on the research of frost and anti/de-icing fluid effects on aircraft wing at take-off.

The research was done by the team of Arteform Oy, headed by MSc Juha Kivekäs.

Helsinki, July 31st 2017

Erkki Soinne
Chief Adviser, Aeronautics
Finnish Transport Safety Agency, Trafi
Index

Nomenclature .............................................................................................................. 4
1 Background ............................................................................................................... 5
2 Computational grids ................................................................................................. 6
3 Description of the simulation cases ......................................................................... 7
4 Results ..................................................................................................................... 9
5 Boundary layer analysis of the flat plate wind tunnel results ............................... 14
6 Comparison of the boundary layer data to the CFD results ................................. 17
7 Conclusions ........................................................................................................... 21
References ................................................................................................................ 22
Appendix I – Overview of the computational grids .............................................. 23
Nomenclature

\( L \)  flat plate length
\( q \)  dynamic pressure \( q = \rho U^2/2 \)
\( Re \)  Reynolds number \( Re = \rho UL/\mu \)
\( t \)  time
\( U \)  velocity
\( x, y, z \)  coordinates

\( \delta^* \)  boundary layer displacement thickness
\( \rho \)  density
\( \mu \)  dynamic viscosity \( \text{note units: N}\cdot\text{s/m}^2 = \text{kg/(m}\cdot\text{s}) = \text{Pa}\cdot\text{s} = 1000 \text{ cP} \)
\( \nu \)  kinematic viscosity \( (\mu/\rho) \) \( \text{note units: m}^2/\text{s} \)
1 Background

The effort to investigate anti/de-icing fluids on a flat plate with an airflow over it using CFD started as part of the Icewing project (see Koivisto and Auvinen). At that point, no wind tunnel tests were yet done. This lead to certain aspects like fluid properties to be overlooked in the simulations while the emphasis was on the simulation methods. Consequently, the comparison of the simulation results to the wind tunnel experiment results was difficult. The effect of the air velocity acceleration and the fluid properties have been checked as part of the Frostwing project and documented in ref. Koivisto and Honkanen.

The simulations have been done with a computational grid that models 0,6-meter-long flat plate. There is also 0,6-meter wind tunnel model and additionally a longer 1,8-meter-long model. The longer model has been used more often than the shorter one. One of the objectives of the research has been to simulate also the longer flat plate to check if there is any Reynolds number effect. This has been postponed by other work, including a grid resolution study (Koivisto and Honkanen) and the already mentioned fluid property checks. The simulation of the longer flat plate is now done and documented in this report, including comparison of the results to the wind tunnel experiments.

As part of the the Icewing project wind tunnel tests were also done with the flat plate models with a boundary layer pressure-rake instrumentation. A summary of the results of these experiments are presented in this report. The boundary layer data is also compared to the CFD results.
2 Computational grids

Two computational grids have been used in the simulations covered in this report. The original grid has been generated with GridPro software and it is 0.6 m in length and 0.5 m in height. The grid also has depth of 1 mm in z-direction resulting in finite volume, as required in all 2D OpenFOAM simulations. This grid has been used in vast majority of the simulations conducted in Icewing and Frostwing projects. The total number of computational cells is approximately 160 000, of which about 80 000 are located in a refined region below the height of 60 mm.

The main issues in generating a longer version of the grid for the 1.8 m flat plate simulations were that the GridPro software was no longer available and a completely new grid would most likely have somewhat different cell geometry in the first 0.6 meters of length. This would lead to an uncertainty because the comparison of this region is the main objective. The problem was resolved by using the OpenFOAM built-in mesh manipulation tools to generate a new longer grid by copying and mirroring the original grid. This work is documented in ref. 1 Honkanen.

The new longer grid is in fact 1.76 m in length, which is 0.04 m shorter due to the compromises involved in the generation process. This difference is however insignificant considering the Reynolds number effect and other objectives. In this report, the longer grid is labeled as 1.8 m, since this is the length of the wind tunnel model. The longer grid has approximately 480 000 cells and has the same topology and cell geometry as the original grid.

Overview of the computational grids is presented in Appendix I. More details and images can be found in refs. 1 Honkanen and 3 Koivisto and Honkanen.
3 Description of the simulation cases

The latest simulation effort has two main objectives. The first is to produce simulation results that could be compared to the results of the wind tunnel experiments. This means matching the fluid properties and dynamic pressure vs. time. The second objective is to compare the CFD results of the 0.6-meter-long flat plate to the 1.8-meter-long version, especially the first 0.6 meters of it. This is to check if the longer plate has an effect that propagates upstream. Also, the outlet boundary condition is much further away from the region of interest in this case.

Since the wind tunnel experiments with the 0.6 m and 1.8 m models were done at different dates, they have slightly different fluid properties. This increased the number of simulation cases in order to avoid uncertainties. Total number of simulation cases is four, including an older reference case C2. The case details are listed in Table 1 and the air velocity ramps are presented in Figure 1.

Table 1. List of simulation cases and fluid properties.

<table>
<thead>
<tr>
<th>Case</th>
<th>Grid</th>
<th>Air velocity ramp</th>
<th>Air density [kg/m³]</th>
<th>Fluid density [kg/m³]</th>
<th>Fluid viscosity [mPas]</th>
<th>Surface tension [N/m]</th>
</tr>
</thead>
<tbody>
<tr>
<td>C2 (ref.)</td>
<td>0.6 m</td>
<td>Non-linear</td>
<td>1.0</td>
<td>1040</td>
<td>21</td>
<td>0.0298</td>
</tr>
<tr>
<td>L06A</td>
<td>0.6 m</td>
<td>WT_fit</td>
<td>1.23</td>
<td>1040</td>
<td>33</td>
<td>0.036</td>
</tr>
<tr>
<td>L06B</td>
<td>0.6 m</td>
<td>WT_fit</td>
<td>1.23</td>
<td>1040</td>
<td>49</td>
<td>0.036</td>
</tr>
<tr>
<td>L18</td>
<td>1.76 m</td>
<td>WT_fit</td>
<td>1.23</td>
<td>1040</td>
<td>49</td>
<td>0.036</td>
</tr>
</tbody>
</table>

Figure 1. Comparison of the velocity ramps used as inflow boundary condition in the CFD simulations.
The results of simulation cases L18 and L06A are compared to their respective wind tunnel test results. Case L18 is also compared with case L06B in order to check the Reynolds number effect with cases which have the same fluid properties. Case C2 from ref. Koivisto and Honkanen is used as a reference case because it represents the status of the simulation work at that time.

Case C2, being an older case, has been simulated for 5 seconds, while the simulation time is 10 or 15 seconds for the new cases. The longer simulation time is required for two reasons. The air velocity ramp for the new cases is fitted to the wind tunnel measurements (ref. Koivisto and Honkanen) and it is less aggressive at the beginning as seen in Figure 1. Secondly, for the case L18 it takes longer for the liquid waves to reach the trailing edge, which is required for comparison to the wind tunnel results.

The computational cost for the cases are presented in Table 2. It should be noted that the case L18 has been computed using 4 CPU cores, but still the cost is higher compared to the other cases.

**Table 2.** Computational cost.

<table>
<thead>
<tr>
<th>Case</th>
<th>Grid</th>
<th>Sim. time [s]</th>
<th>Comp. time [h]</th>
<th>Cost [h/s/CPU]</th>
<th>CPU cores</th>
</tr>
</thead>
<tbody>
<tr>
<td>C2 (ref.)</td>
<td>0,6 m</td>
<td>5.0</td>
<td>263</td>
<td>26</td>
<td>2</td>
</tr>
<tr>
<td>L06A</td>
<td>0,6 m</td>
<td>10.0</td>
<td>663</td>
<td>33</td>
<td>2</td>
</tr>
<tr>
<td>L06B</td>
<td>0,6 m</td>
<td>10.0</td>
<td>669</td>
<td>33</td>
<td>2</td>
</tr>
<tr>
<td>L18</td>
<td>1,76 m</td>
<td>15.0</td>
<td>4029</td>
<td>67</td>
<td>4</td>
</tr>
</tbody>
</table>
4 Results

The total liquid volume on the flat plate reduces as the liquid is driven off the plate by the air flow. For the 0.6-meter flat plate results of the case L06A and the results of Type I de-icing fluid wind tunnel tests on 7.5.2015 are compared in Figure 2. The total liquid volume remaining in % and the dynamic pressure of the air flow in Pa x 10 are shown in the vertical axis. The horizontal axis shows time which is the same for simulation and wind tunnel results because of the matched inflow velocity.

Since the velocity ramp and air density of 1.23 kg/m$^3$ used in the simulations have been matched to the wind tunnel test, the agreement of the dynamic pressure is excellent. The fluid removal begins at about t = 4.5 s in the simulation while in the experiment removal is observed already at t = 2.5 s. After 6 seconds of simulation time, the simulation results and the wind tunnel test results are in excellent agreement.

![Comparison of the simulation results to the wind tunnel results for the 0.6 m flat plate](image)

**Figure 2.** Comparison of the simulation results to the wind tunnel results for the 0.6 m flat plate (Type I fluid, date 7th May 2015).

The same velocity ramp was used in the simulation case L18 of the 1.8 m flat plate. The results are compared to the wind tunnel test of Type I de-icing fluid on 1.4.2015 in Figure 3. There is some variation in the spool-up of the wind tunnel fan resulting in slightly different velocity ramp profiles. The agreement of the dynamic
pressure in the simulation L18 and the wind tunnel tests is still very good and the differences can be considered negligible. Similar behavior to the 0.6 m flat plate simulation is observed, except it takes longer time (11-12 seconds) for the liquid volume to reach the same level as in the wind tunnel test. The liquid removal begins later in case L18 compared with L06A since the waves are the primary mover of the fluid and it takes longer for the waves to reach the trailing edge in the case L18.

![Graph](image)

**Figure 3.** Comparison of the simulation results to the wind tunnel results for the 1.8 m flat plate (Type I fluid, date 1\textsuperscript{st} April 2015).

Several reasons for the differences between the measured and the simulated results observed in Figures 2 and 3 can be identified:

- The initial condition in the simulations is very static, while there are initial disturbances in the wind tunnel due to the idling of the wind tunnel fan.
- The resolution of the computational grid is insufficient to capture small waves. The results from the grid resolution study (ref. Koivisto and Honkanen) show that the removal is faster for the case with the refined grid.
- The initial thickness of the fluid was exactly 1 mm in the simulations. The initial thickness of the fluid in the wind tunnel tests is more approximately defined. The initial thickness has an effect on wave height and wave speed and therefore on the removal rate.
- The waves in the simulations are formed at the leading edge of the fluid layer and they must travel the entire plate, while waves are formed all over the flat plate in the wind tunnel test. After the simulations have reached a point where there are waves along the entire length of the flat plate, the removal rate increases.
The total liquid volume on flat plate for the CFD cases with the 0.6 m grid is presented in Figure 4. Clearly the fluid removal in the reference case C2 is totally different compared to the new cases L06A and L06B. Many details in the case setup are different. In the case C2 the entire computational domain was initialized with velocity of 2 m/s. This leads to the rapid removal of the liquid in the very beginning of the simulation. As shown in Figure 1 the non-linear velocity ramp in C2 is more aggressive compared to the wind tunnel fitted acceleration profile in cases L06A and L06B. The air density (1.0 vs. 1.23 kg/m$^3$) and fluid viscosity (see Table 1) are also different.

The only difference between the cases L06A and L06B is the viscosity of the fluid, which is 33 mPas in L06A and 49 mPas in L06B. This shows similar effect as the case NU in ref. 4 Koivisto and Honkanen, Figure 1. The rate of the liquid removal (slope of the curve) at $t = 5.5$ s is lower in L06B because of the higher viscosity. This accumulates to a difference of ~5 %-units in the liquid volume compared to L06A that remains approximately constant between $t = 6.5 \ldots 10.0$ seconds.

Figure 4. Total liquid volume % on the flat plate over time for cases C2, L06A, and L06B.

The average flowrate of the liquid removal is considerably different in the reference case C2. The 1-second and 0.2-second moving averages of the removal rate in %/s are presented in Figure 5 for cases C2 and L06A. The removal of the liquid by the waves is more pronounced by the 0.2-second moving average curves while the 1-second average has a strong smoothing effect.
Finally, the results of the case L06B are compared to the first 0,6 meters of the case L18 in Figure 6. Both cases have the same fluid properties. Here the vertical axis shows the nominal thickness of the fluid layer on the flat plate. Since the total liquid volume fraction is output to file by the CFD solver, further post-processing is needed to determine the absolute volume on only a part of the flat plate, the first 0,6 meters of the longer plate in this case. The nominal thickness represents the absolute liquid volume scaled as thickness, not taking into account wave height (thickness distribution).
Small differences can be observed in Figure 6, and the longer plate seems to add resistance that leads to slightly less fluid to be removed than in the case L06B with the computational domain ending at x = 0.6 m. However, the different post-processing method used to obtain the partial volume in the case L18 could lead to inaccuracies of the same magnitude as the difference seen in Figure 6. There are also small qualitative differences as shown in Figure 7 which is an overview of the fluid interface at t = 5 s.

Figure 7. Overview of the fluid interface in cases L06B, and L18 at t = 5 s, between x = 0 … 0.6 meters.

The very slow computation of the case L18 is due to the break-up of the fluid interface. The wave crests are broken and the splashes of the fluid fly in the air and hit the fluid bed causing further disturbances. An example of this phenomenon is shown in Figure 8 at t = 7.6 s. The break-up is problematic for the solver, because the volume-of-fluid method used to define the phase interface in the simulation is unable to track the rapid changes caused by the splashes.

Figure 8. Break-up of the waves in the case L18 at t = 7.6 s, between x = 0.9 … 1.2 meters.
5 Boundary layer analysis of the flat plate wind tunnel results

To study the effects of moving fluid layer on the boundary layer of the accelerating airflow over it there was a boundary layer rake assembled at the trailing edge of the flat plate as shown in Figure 9. The rake geometry is shown in Figure 10. To avoid building a second rake for the shorter plate the rake could be tilted to a 45° angle which enabled a thinner boundary layer to be measured with a reasonable accuracy.

Figure 9. Boundary layer pressure rake location on the 1,8 m flat plate wind tunnel model. The rake is situated on the trailing edge of the shorter 0,6 m model as shown by the arrow in the picture.

Figure 10. Boundary layer rake tube geometry at 90° angle. Topmost tube is the static pressure reference.

To avoid the moving fluid to clog the lowest pitot tubes they were sealed. For the 0,6 m plate the 4 lowest tubes were sealed whereas for 1,8 m plate the 6 lowest tubes were sealed. When calculating the boundary layer thickness the pitot pressure at the lowest tubes had to be extrapolated using the data from the open tubes. This naturally includes an unknown error source.

In the de/anti-icing aerodynamic acceptance test (SAE AS 5900) the fluid aerodynamic effect is defined by measuring the boundary layer displacement thickness of
the air flow. Displacement thickness was therefore also of primary interest in the boundary layer measurements in this study. To assess the results the measured displacement thickness at the trailing edge of an uncontaminated clean flat plate were compared with theoretical boundary layer calculations. In Figure 11 and Figure 12 the measured displacement thicknesses are compared with values calculated from the well-known formula of Prandtl for a turbulent boundary layer (refs. 6White, p. 434, eq. 670 & 5Schlichting, p. 638, eq. 21.6):

\[
\frac{\delta^*}{x} = 0.02/Re_x^{1/7}
\]  

(1)

The figures show that for the 1,8 m flat plate the measured displacement thicknesses are in a good agreement with the values of equation (1), however the measured displacement thicknesses of 0,6 m flat plate are more than 30 % higher than the values given by equation (1).

**Figure 11.** Wind tunnel speed (blue), calculated boundary layer displacement thickness (red) and measured boundary layer displacement thickness at the trailing edge of the 1,8 m flat plate.

**Figure 12.** Wind tunnel speed (blue), calculated boundary layer displacement thickness (red) and measured boundary layer displacement thickness at the trailing edge of the 0,6 m flat plate.
The discrepancy between the measured and calculated displacement thicknesses may be due to different leading edge geometries between the two plates, which are hand finished. The 0.6 m plate leading edge may cause a laminar separation bubble large enough to increase the boundary layer displacement thickness. However, this explanation is not verified by any means.
6 Comparison of the boundary layer data to the CFD results

Boundary layer data of the Type I anti-icing wind tunnel test of 7th May 2015 is compared with the CFD case L06A which has been simulated with the same flow properties. The CFD result data has been saved at 0,005 second intervals, matching the rake measurement frequency of 200 Hz. The velocity data is probed from same locations as the boundary layer rake tubes were on the wind tunnel model. The velocity profile is averaged over t = 7,0 ... 7,2 seconds in the CFD simulation and therefore it consists of 40 time samples. The inflow velocity is approximately 22,5 – 23 m/s (q ≈ 310 Pa) at this time interval.

The measured velocity profiles at the trailing edge (x = 0,585 m from the leading edge) are presented in Figure 13. Included are one dry wind tunnel run without fluid, two runs with fluid (same runs as in Figure 2). Note that the air velocity in two points nearest of the wall are not measured (distance from the wall 0 and 0,18) and in the four next points from the wall are extrapolated values as the pitot tubes have been sealed.

![Figure 13](image)

**Figure 13.** Comparison of the measured velocity profiles at the trailing edge of the 0,6 m flat plate (x = 0,585 m from the leading edge).

Figure 14 shows comparison of the mean value of the CFD calculations of the case L06A between time period t = 7...7,2 s to the wind tunnel runs. The shape of CFD mean velocity profile differs significantly from the measured ones.
Figure 14. Measured velocity profiles for the two fluid runs compared to mean velocity profile of the CFD case L06A over time period t = 7...7.2 s.

There are strong fluctuations in the CFD velocity due to the air vortices. This is visible in the mean CFD velocity curve which shows a higher velocity in the $y = 10$ mm region compared to the free flow. To illustrate these fluctuations Figure 15 and Figure 16 show the velocity profile combined with the corresponding wave positions at time instants $t = 7.08$ s and 7.125 s. The vicinity of the wave seems to intensify the effect of a vortex on the velocity profile.
Figure 15. Measured velocity profiles compared to CFD velocity profiles at time points $t = 7.08$ s and $7.125$ s.

Figure 16. Velocity calculation line at $x = 0.585$ m ("probe position") relative to wave positions at time instants $t = 7.08$ and $7.125$ s.
The displacement thicknesses calculated from velocity profiles of Figure 14 are:

- wind tunnel run 1 (@ ~23 m/s): \( \delta^* = 4.0 \) mm
- wind tunnel run 2 (@ ~23 m/s): \( \delta^* = 4.7 \) mm
- CFD mean velocity (@ 7...7,2 s, ~23 m/s): \( \delta^* = 3.0 \) mm

There are many potential reasons for large deviations between measured and CFD simulation results within the boundary layer:

- 2D LES model with SGS – model may fail in results in the boundary layer near the wall (in this case near the fluid layer).
- The CFD computational grid may not be optimal for boundary layer calculations.
- Pitot tube measurements act as an efficient filter for frequencies higher than 10 to 100 Hz while the calculated fluctuations are at frequencies of one to two orders of magnitude higher.
- The presence of the rake assembly could interfere with the air vortices making their measurement difficult.
- Since the pitot tubes of the rake are designed to measure total pressure of the flow in direction approximately parallel to the tubes, it is questionably if measurement of the vortex street is possible due to the large variations in the local flow direction.
- Considering the differences between measurements for uncontaminated 0,6 m and 1,8 m flat plates the 0,6 m plate results are worse when compared to analytical solutions. The reason for this remains unknown.
7 Conclusions

The case L06A has been simulated with matching fluid and flow properties to produce simulation results that would be fully comparable to the wind tunnel experiments. The fluid flow-off results are in very good agreement. The longer 1.8 m flat plate has been simulated for the first time (case L18). The simulation was very time consuming but eventually after 12 seconds of simulation time the total volume reached the same level as in the measurements. From this point until the end of the simulation at 15 seconds, the agreement with the measurements is very good. Overall the shape of the flow-off curve is similar between the 0.6 m and the 1.8 m cases. There is a similarly slow flow rate to be observed in the beginning of the case L18 as in the case L06A, and the case L06B with fluid properties of L18. There are still uncertainties that could explain this phenomenon, including the instability of the measured liquid due to wind tunnel idling compared to the mathematically accurate steady initial condition in the simulations. In the simulations the waves are formed at the leading edge only and they must travel longer distance from the leading edge to the trailing edge in the case L18.

Any upstream effect of the higher Reynolds number was deemed negligible when the first 0.6 meters of the longer case were compared to the case L06B. This suggests that the outlet boundary condition does not have a negative effect in the simulations.

The comparison of the measured boundary layer rake results to the simulations proved challenging. The velocity was probed directly from the simulations while dynamic pressure was measured using the rake. Even though the sampling frequency was 200 Hz in both simulations and measurements, the air vortices are clearly visible only in the CFD velocity profiles. The air vortices are strong and frequent enough to distort the mean velocity profile. A longer sampling time could be used, but the accelerating air flow adds another uncertainty in this case.
References

Appendix I – Overview of the computational grids

Figure 17. Overview of the original 0,6-meter flat plate grid with approximately 160 000 cells.
Figure 18. Overview of the 1,76-meter flat plate grid with approximately 480 000 cells.